MATH 162 Quiz 3 NAME:

1. Solve the inequality, $\frac{x-2}{x^2-3x-10} \ge 0$.

Solution:

$$\frac{x-2}{x^2 - 3x - 10} \ge 0$$
$$\frac{x-2}{(x-5)(x+2)} \ge 0$$

Checking the signs of x-2, x-5 and x+2 over the regions $(\infty, -2)$, (-2, 2), (2, 5) and $(5, \infty)$, we conclude that $(-2, 2] \cup (5, \infty)$ is the solution set.

2. Solve for x, $\sqrt{7x+2} + x = 6$.

Solution:

$$\sqrt{7x+2} + x = 6$$

$$\sqrt{7x+2} = 6 - x$$

$$(\sqrt{7x+2})^2 = (6-x)^2$$

$$7x+2 = 36 - 12x + x^2$$

$$(x-2)(x-17) = 0.$$

Substituting x=2 and x=17 into the original equation, we find the solution to be x=2.

3. Given A(1,5) and B(2,-2), find (a) the distance d(A,B) and (b)the midpoint of segment AB.

Solutions: $d(A,B) = \sqrt{(1-2)^2 + (5-(-2))^2} = \sqrt{50}$. Also the midpoint is $(\frac{1+2}{2}, \frac{5+(-2)}{2}) = (\frac{3}{2}, \frac{3}{2})$.