

MATH 212 Quiz 4 NAME:

1. Sketch the curve $r = 1 - \sin \theta$.
 - It is a cardioid. Consult the textbook.
2. Find the area of the region enclosed by the polar curve given in exercise #1.
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$$\begin{aligned} \text{Area} &= \frac{1}{2} \int (1 - \sin \theta)^2 d\theta \\ &= \frac{2}{3} \theta + 2 \cos \theta - \frac{\sin 2\theta}{4} \Big|_0^{2\pi} \\ &= \frac{3}{2} \pi. \end{aligned}$$

3. Find all points of intersection of $r = \sin \theta$ and $r = \cos \theta$. Sketch both graphs.
 - The points of intersections are $(r, \theta) = (0, 0)$ and $(\frac{1}{\sqrt{2}}, \frac{\pi}{4})$.